



FIGURE 1. The (collapsing) Mackey functor slice spectral sequence for  $H\underline{\mathbf{Z}} \wedge \bigvee_{n \in \mathbf{Z}} S^{n\rho_2}$ . The symbols are defined in Table 2.

In other words the  $RO(G)$ -graded Mackey functor valued homotopy of  $H\underline{\mathbf{Z}}$  is as follows. For  $n > -3/2$  we have

$$\pi_i \Sigma^{n\rho_2} H\underline{\mathbf{Z}} = \pi_{i-n\rho_2} H\underline{\mathbf{Z}} = \begin{cases} \square & \text{for } n \text{ even and } i = 2n \\ \bullet & \text{for } n \text{ even and } i = 2n - 2j \text{ with } 0 < j \leq n/2 \\ \square & \text{for } n \text{ odd and } i = 2n \\ \bullet & \text{for } n \text{ odd and } i = 2n + 1 - 2j \\ & \text{with } 0 < j \leq (n+1)/2 \\ 0 & \text{otherwise} \end{cases}$$

For  $n < -3/2$  we have

$$\pi_i \Sigma^{n\rho_2} H\underline{\mathbf{Z}} = \pi_{i-n\rho_2} H\underline{\mathbf{Z}} = \begin{cases} \blacksquare & \text{for } n \text{ even and } i = 2n \\ \bullet & \text{for } n \text{ even and } i = 2n + 2j - 1 \\ & \text{with } 0 < j \leq (-3-n)/2 \\ \square & \text{for } n \text{ odd and } i = 2n \\ \bullet & \text{for } n \text{ odd and } i = 2n + 2j \\ & \text{with } 0 < j \leq (-3-n)/2 \\ 0 & \text{otherwise} \end{cases}$$

We can use Definition 8 to name some elements of these groups.

Note that  $H\underline{\mathbf{Z}}$  is a commutative ring spectrum, so there is a commutative multiplication in  $\pi_* H\underline{\mathbf{Z}}$ , making it a commutative Green functor. For such a functor  $\underline{M}$  on a general group  $G$ , the restriction maps are a ring homomorphisms while the transfer maps satisfy the Frobenius relations (1).